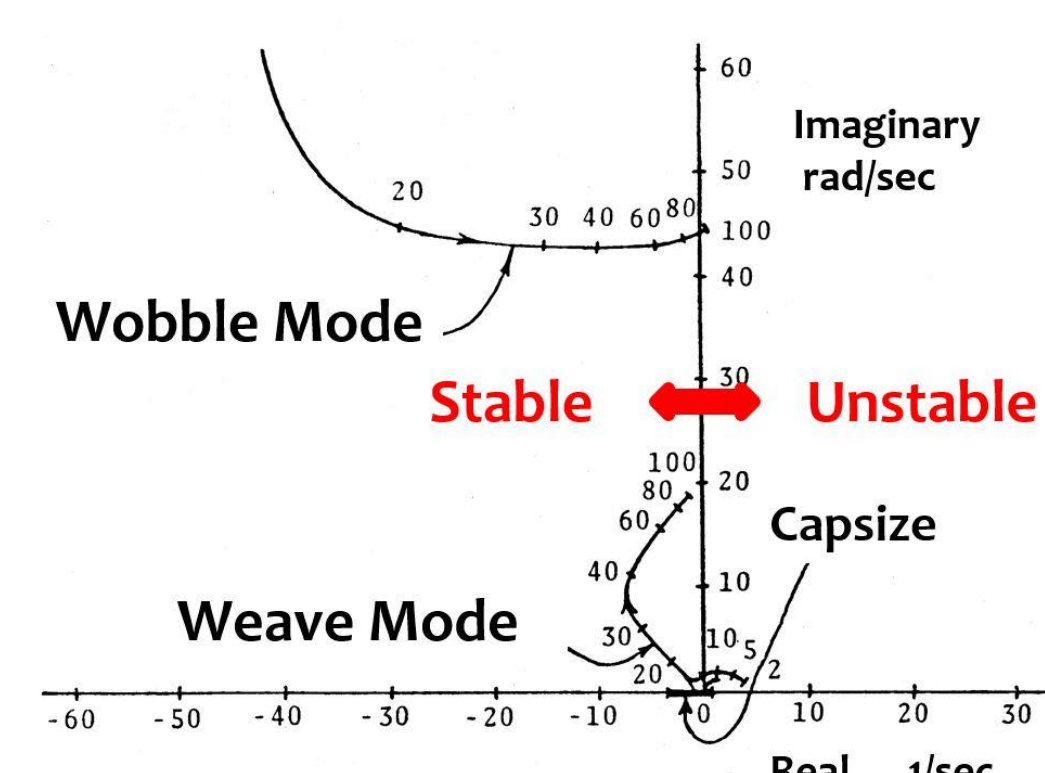


# Analysis of High Speed Wobble Mode using Energy Flow Method

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## Introduction & Objectives : Detailed mechanism of high speed instability of wobble mode

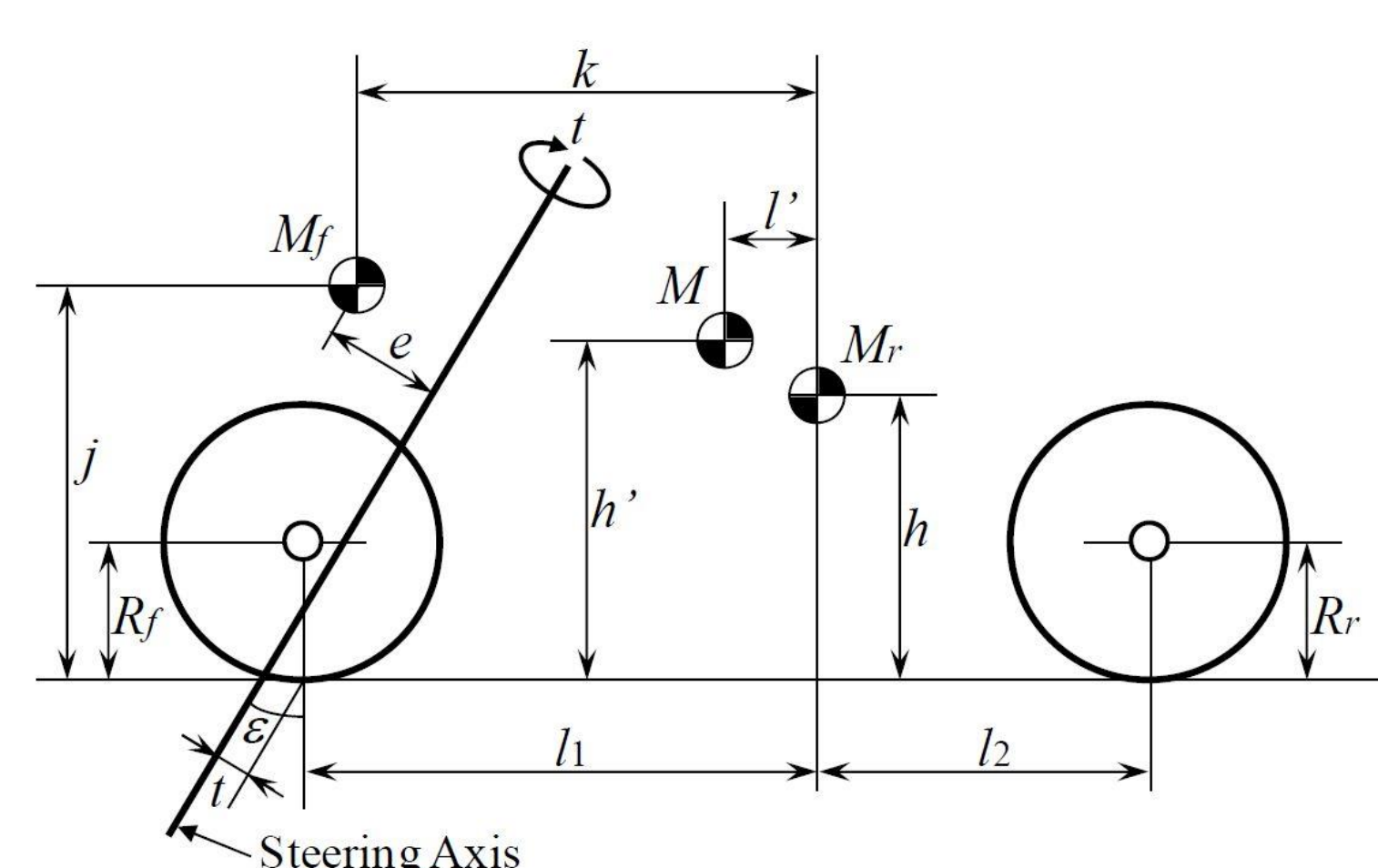
Motorcycles have instability modes at high speed range. These are called wobble and weave modes. The reasons of the **high speed instabilities** have not been understood by now.



Shows that the detailed mechanism of high speed instability of wobble mode **in a context of equations of motion**.

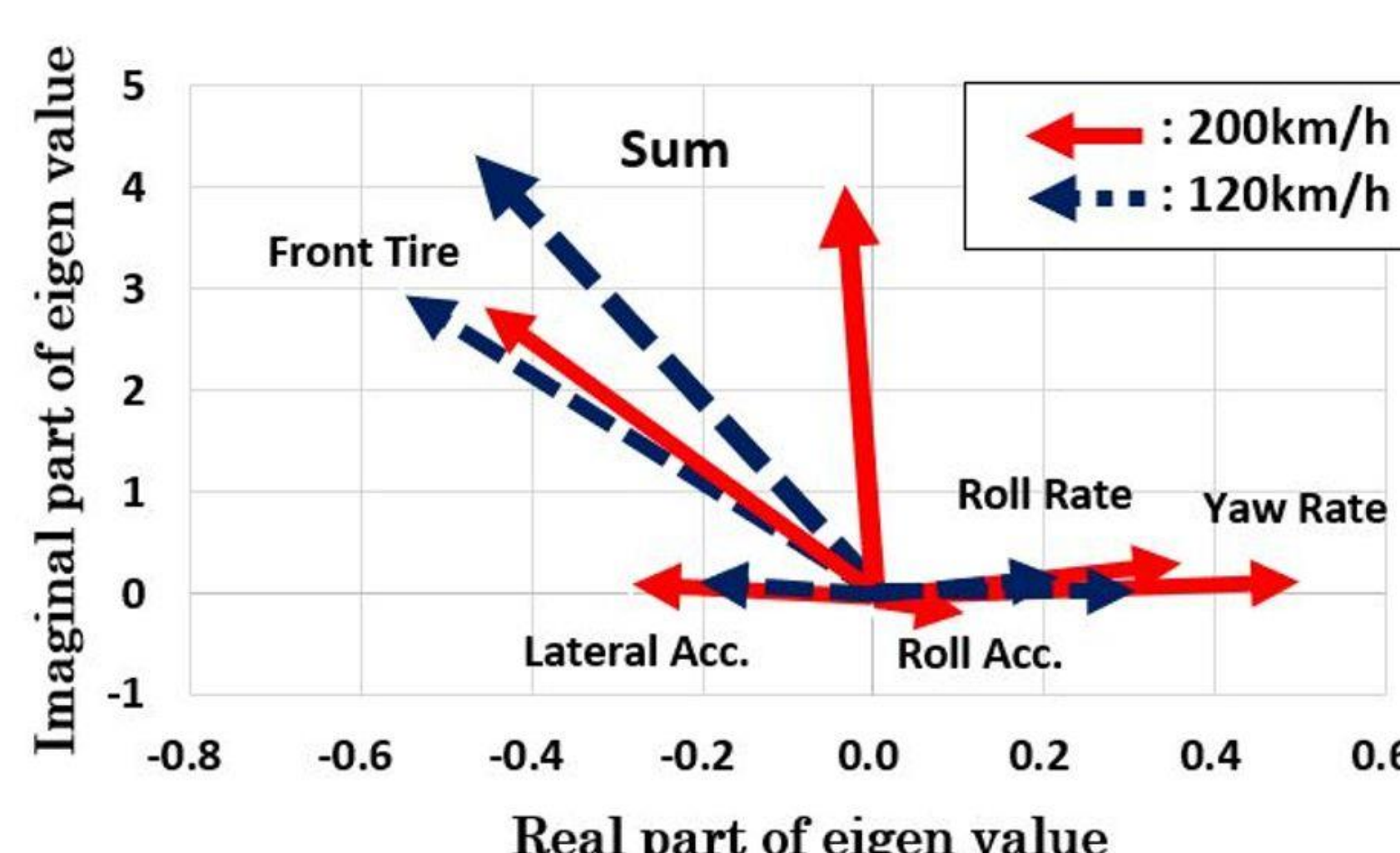
## Method : Energy flow method using eigenvectors

### (1) Computation Model [1]

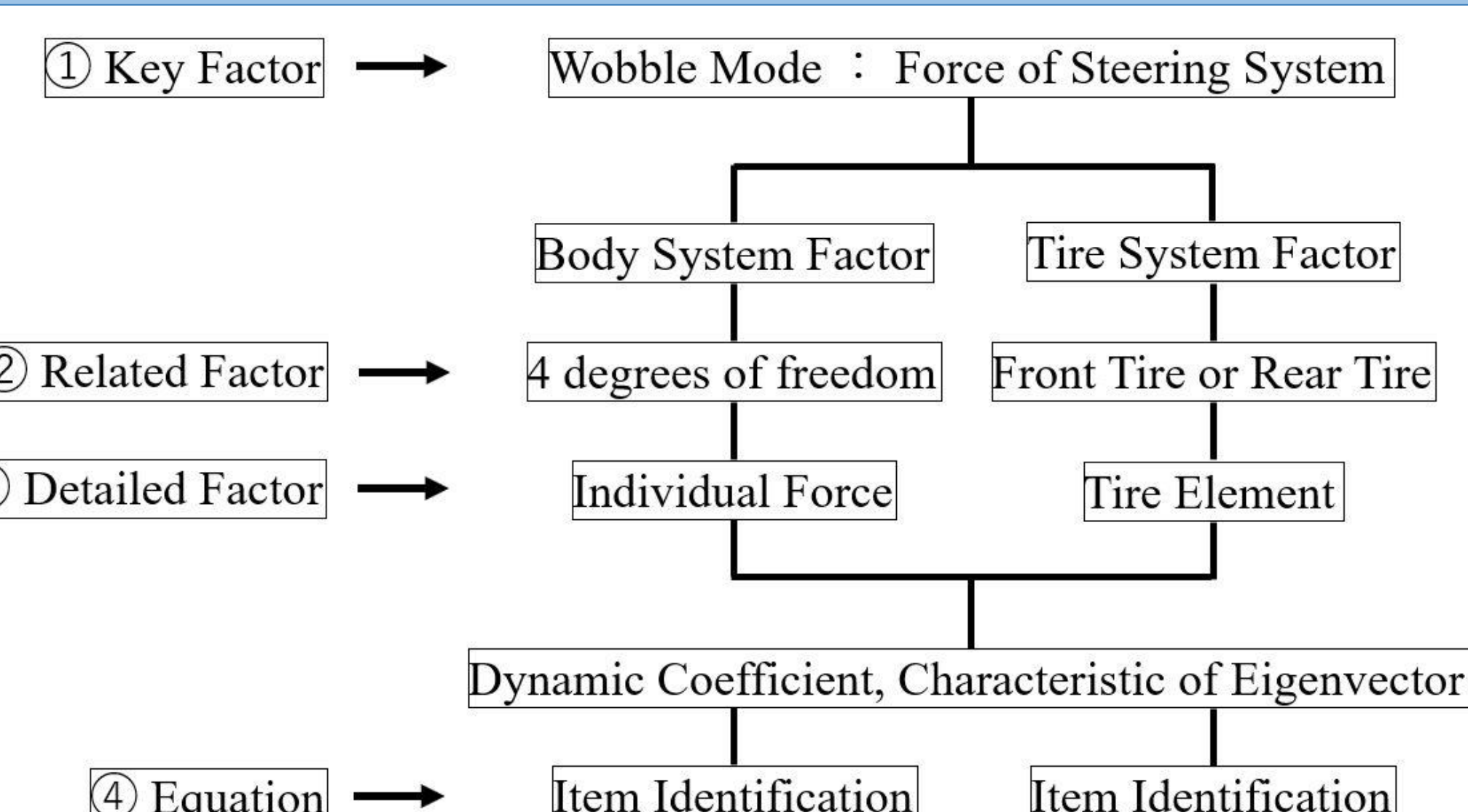


Mathematical model

### (2) Configuration of Torques Acting on Steer [2,3]



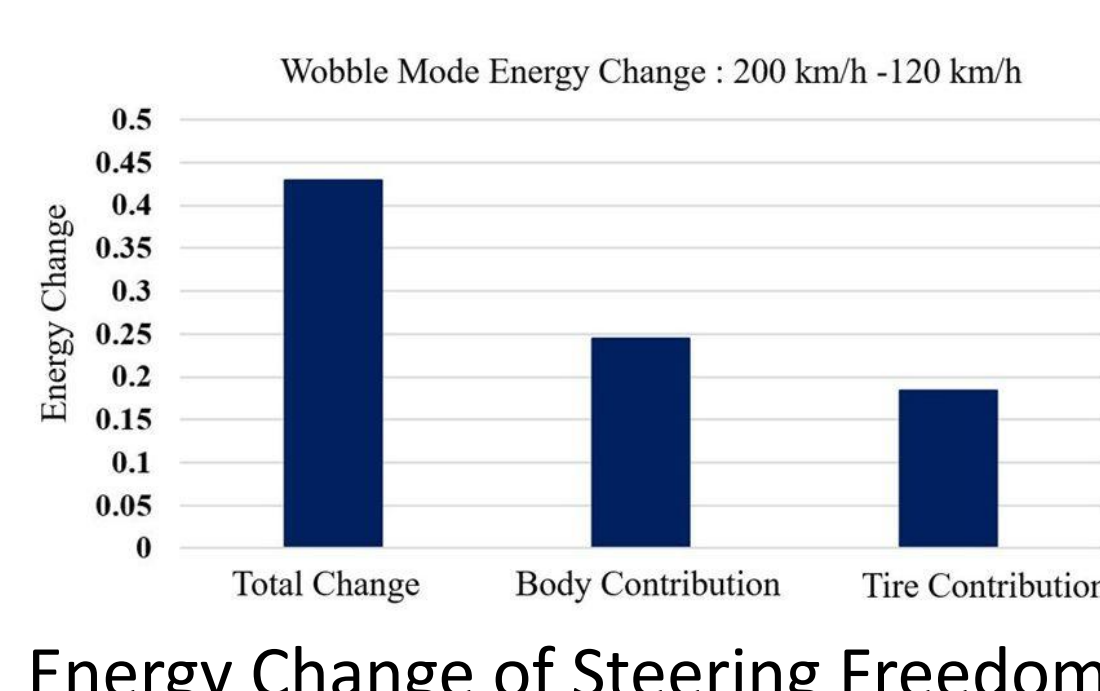
### (3) Flow of Methods to Find the Cause of Straight-line Stability Change



## Result : Analysis of High Speed Wobble Modes

### (1) Key Factor

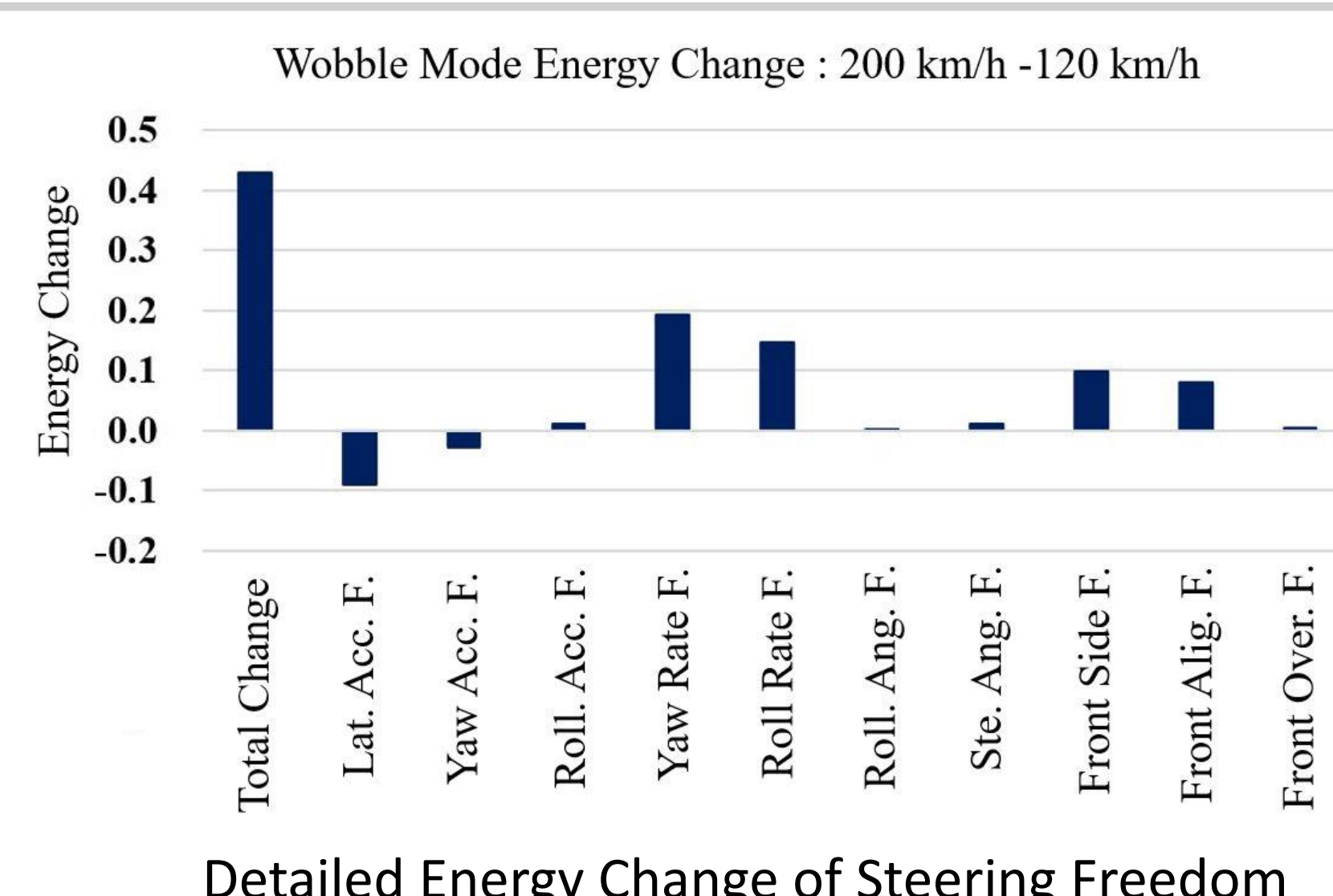
Increased **body system energy**.



Energy Change of Steering Freedom

### (2) Related Factor

In the vehicle system, **yaw rate force** and **roll rate force** contribute to destabilization.

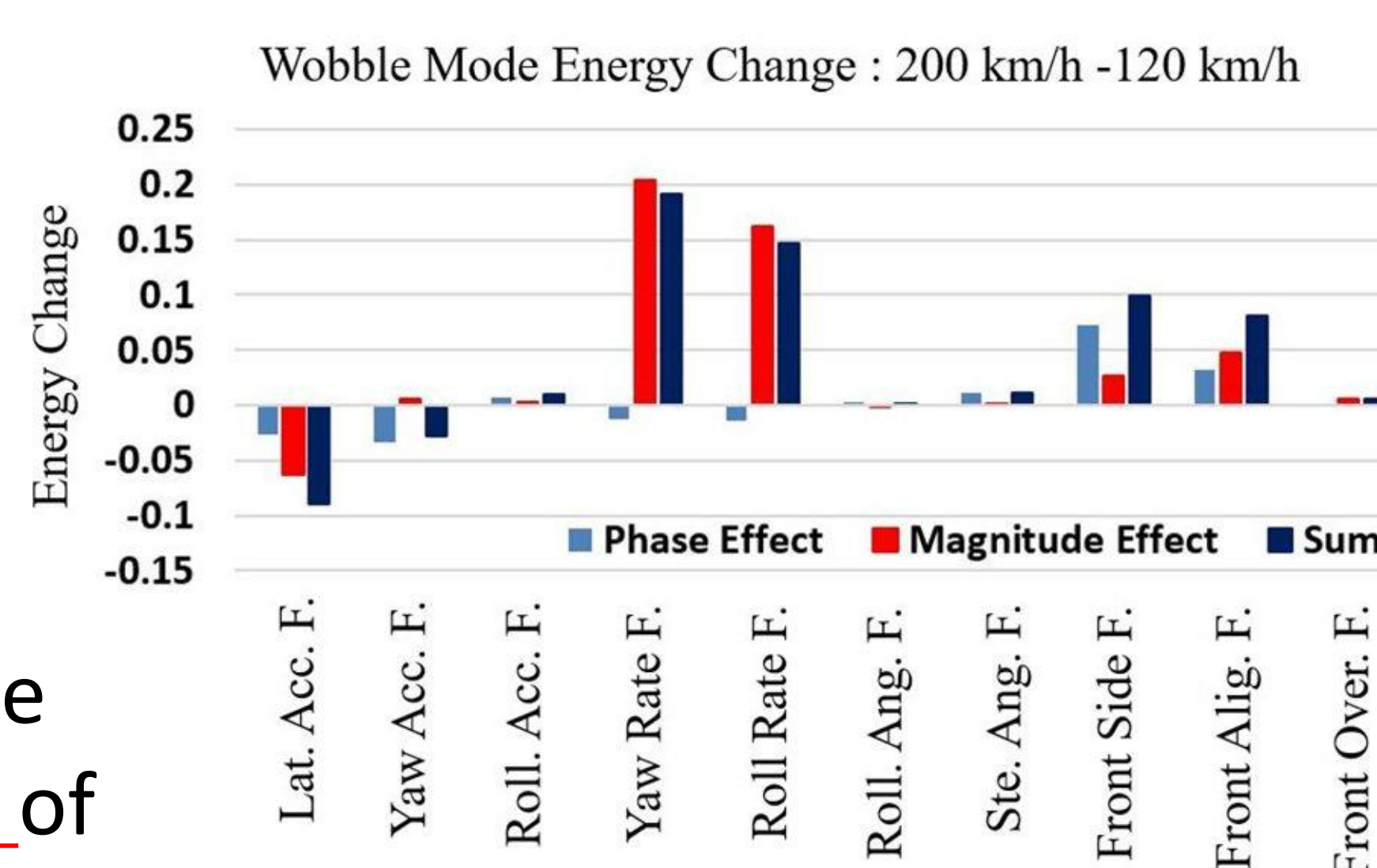


Detailed Energy Change of Steering Freedom

### (3) Detailed Factor

Compare vehicle system contributions by effect. (**Phase Effect** and **Magnitude Effect**)

In the vehicle system, the **effect of the magnitude** of the **yaw rate force** and **roll rate force** is main.



Two Effects of Acting Forces on Steering Freedom (Phase Effect and Magnitude Effect)

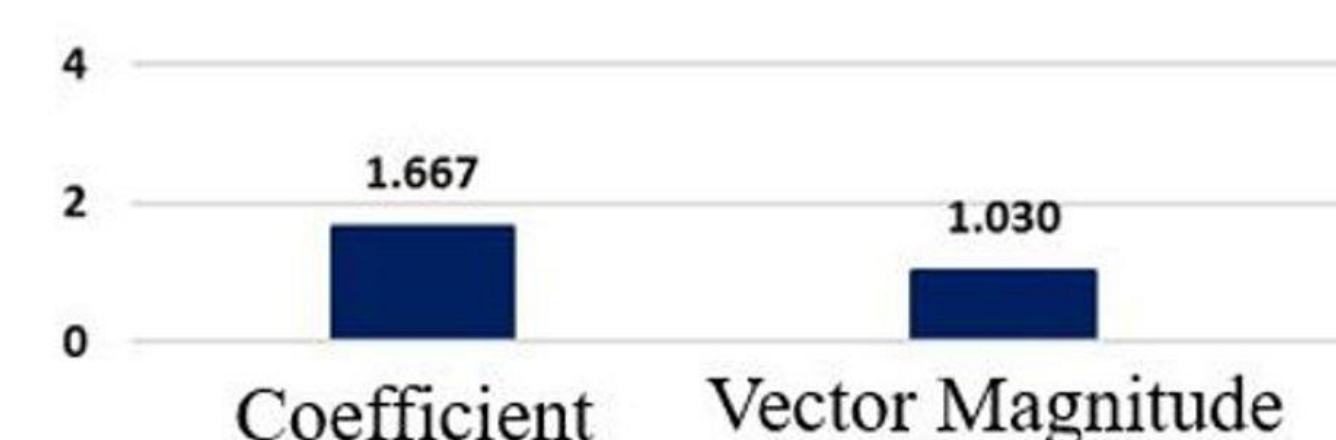
### (4) Equation

The reasons of the high speed instabilities  
• Consideration of only **magnitude effect**

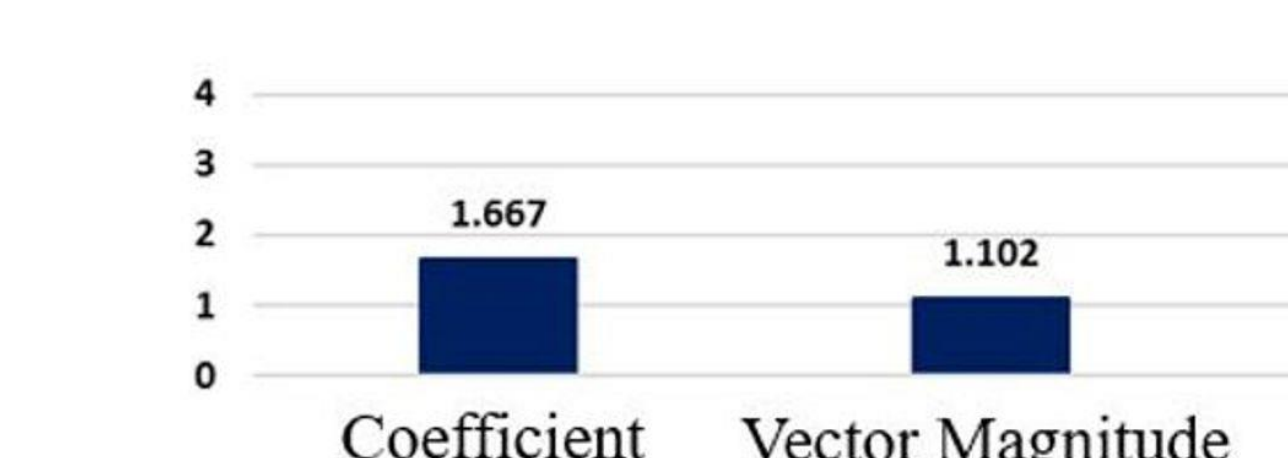
$$M_f e \ddot{y}_1 + (M_f e k + I_{fz} \cos \varepsilon) \ddot{\psi} + (M_f e j + I_{fz} \sin \varepsilon) \ddot{\phi} + (I_{fz} + M_f e^2) \ddot{\delta} + (M_f e + i_{fy}/R_f \sin \varepsilon) \dot{x}_1 \dot{\psi} - i_{fy}/R_f \cos \varepsilon \dot{x}_1 \dot{\phi} + (tZ_f - M_f e g) \dot{\phi} + (tZ_f - M_f e g) \sin \varepsilon \dot{\delta} + tY_f - T_{zf} \cos \varepsilon - T_{xf} \sin \varepsilon = 0$$

Steering motion

- The magnitude effect is composed of **the coefficient** part of the equation and the **magnitude of the eigenvector**.
- The vehicle body factor is the speed term included in the coefficient of **yaw rate force** and **roll rate force**.



Coefficient and Eigen Vector Change Concerning Yaw Rate Force Acting to Steering Freedom



Coefficient and Eigen Vector Change Concerning Roll Rate Force Acting to Steering Freedom

$$+ (M_f e + i_{fy}/R_f \sin \varepsilon) \dot{x}_1 \dot{\psi}$$

About 58%

$$- i_{fy}/R_f \cos \varepsilon \dot{x}_1 \dot{\phi}$$

100%

Physically, **gyro torque** increases as vehicle speed increases.

## Conclusion

- A major factor for destabilization is the **increase in energy in the body system**.
- The **yaw rate force** and **roll rate force** acting on **the steering system** are increased.
- The reason is that the **gyro torque** increases included in the yaw rate force and roll rate force.
- At higher speeds, the gyro torque increases as the wheel speed increases.

## References

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- (2) T. Katayama and T. Nishimi : Energy Flow Method for the Study of Motorcycle Wobble Mode, Vehicle System Dynamics, Vol.19, No.3, p.151-175 (1990)
- (3) Y. Marumo and T. Katayama : Analysis of Motorcycle Weave Mode by Using Energy Flow Method, Transactions of the Japan society of mechanical engineers. C, Vol.77, No.781, p.3490-3501 (2011)